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# Joint maximum likelihood time-delay estimation for LTE positioning in multipath channels

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## Abstract

This paper presents a joint time-delay and channel estimator to assess the achievable positioning performance of the Long Term Evolution (LTE) system in multipath channels. LTE is a promising technology for localization in urban and indoor scenarios, but its performance is degraded due to the effect of multipath. In those challenging environments, LTE pilot signals are of special interest because they can be used to estimate the multipath channel and counteract its effect. For this purpose, a channel estimation model based on equi-spaced taps is combined with the time-delay estimation, leading to a low-complexity estimator. This model is enhanced with a novel channel parameterization able to characterize close-in multipath, by introducing an arbitrary tap with variable position between the first two equi-spaced taps. This new hybrid approach is adopted in the joint maximum likelihood (JML) time-delay estimator to improve the ranging performance in the presence of short-delay multipath. The JML estimator is then compared with the conventional correlation-based estimator in usual LTE conditions. These conditions are characterized by the extended typical urban (ETU) multipath channel model, additive white Gaussian noise (AWGN) and LTE signal bandwidths equal to 1.4, 5 and 10 MHz. The resulting time-delay estimation performance is assessed by computing the cumulative density function (CDF) of the errors in the absence of noise and the root-mean-square error (RMSE) and bias for signal-to-noise ratio (SNR) values between  $-20$  and  $30$  dB.

**Keywords:** LTE; Positioning; OFDM modulation; Positioning Reference Signal (PRS); Multicarrier signal; Multipath channel modelling; Joint time-delay and channel estimation; Ranging

## 1 Introduction

Navigation and positioning technologies are every day more important in civil applications, demanding enhancements on accuracy, availability and reliability. Positioning improvements are mainly achieved, thanks to the advances in Global Navigation Satellite Systems (GNSS) and the introduction of new systems, such as Galileo. However, a myriad of possible working conditions are faced in ubiquitous positioning, where the GNSS nominal performance is highly degraded, such as in urban environments or indoors. Thus, the use of complementary terrestrial localization systems is envisaged as a major step towards the realization of anywhere and anytime

positioning. A relevant example of these technologies is the Long Term Evolution (LTE), a next-generation mobile communications system with promising perspectives on positioning. Indeed, the LTE standard [1,2] specifies a dedicated downlink reference signal for observed time difference of arrival (OTDoA) localization, i.e. the positioning reference signal (PRS). The LTE OTDoA method is based on the time-delay estimation (TDE) of the signals received from different source transmitters (i.e. cellular base stations). Since the LTE downlink signal is based on the orthogonal frequency division multiplexing (OFDM) modulation, the TDE is typically performed with the LTE pilot subcarriers in the frequency domain. Using this method, recent research studies, such as those in [3-5], have shown the potential of LTE to provide accurate positioning. However, multipath propagation and non-line-of-sight conditions are still the main limiting factors in urban

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environments, once inter-cell interference is removed. Therefore, countermeasures against multipath are needed in order to achieve the ultimate positioning performance in LTE.

In order to properly understand and mitigate the effect of multipath, it is important to have a good characterization of the propagation conditions and reflect them on the estimation model of the receiver. Many channel models have been proposed to characterize the propagation conditions of the possible LTE working scenarios. Among them, the LTE standard adopted an extension of the tapped-delay line (TDL) channel models specified for the second- and third-generation mobile systems, i.e. Global System for Mobile communications (GSM) and Universal Mobile Telecommunications System (UMTS). One of these propagation models is the extended typical urban (ETU) model, described in Annex B of [6] and [7]. The ETU model is of special interest because it defines a power-delay profile (PDP) with a line-of-sight (LoS) signal more attenuated (in average) than the multipath rays. This is a representative example of harsh conditions where LTE is expected to be used. In these conditions, the ranging performance of the correlator or matched filter is relatively poor [8]. The correlation-based TDE can be considered as a conventional time-delay estimation method due to its low complexity, being the maximum likelihood (ML) estimator in additive white Gaussian noise (AWGN) channels. However, in multipath channels, the delayed reflections of the signal induce a notable bias on this conventional estimation. Thus, another estimator is required in order to improve the TDE performance in multipath environments.

The time-delay estimation can be enhanced by model-based estimators. These estimators use channel estimation models in order to counteract the effect of multipath. The aim of these models is to characterize the response of the channel, instead of identifying the physical multipath components of the specific environment. There are many possibilities for these channel estimation models. On the one hand, the most accurate model corresponds to the estimation of amplitude, phase and delay of every propagation ray. However, it is also the most complex model because of the many unknowns to estimate. Despite its complexity, this estimation model has been widely studied, for instance, with super-resolution techniques in [9,10], with the ML criterion in [11], or in a two-step approach in [12]. On the other hand, channel estimation models can be simplified by defining equi-spaced or periodic taps relative to the time delay of the first path. Since this model is based on the uniform sampling of the channel, it has been used with the compressed sampling theory for channel estimation, such as in [13,14], but it can also be found in multipath interference cancellation [15].

Timing synchronization for data transmission does not need to achieve the extreme accuracy required for positioning. This is the reason why, in communication applications, the ML approach is widely applied to channel estimation assuming the time delay to be coarsely corrected in a previous stage, and the residual time delay is considered negligible. There are still some contributions that propose the joint maximum likelihood (JML) estimation of the time delay and channel response in OFDM systems, considering a model based on equi-spaced or periodic taps, but few of them deal with the specific case of ranging applications. The authors of [16] propose an algorithm based on the JML approach and on the channel length estimation, but providing only coarse timing estimates. In [17], two JML estimators are applied for synchronization of multiple users. The first one is a joint frequency and channel estimator, while the second one is a joint time-delay and channel estimator. A similar JML approach is used for ranging purposes considering an IEEE 802.16 system [18]. An approximation of the JML algorithm is proposed in [19] using early and late estimations in a delay lock loop (DLL). The JML estimation has also been studied for multicarrier ranging considering the optimal placement of pilot subcarriers in [20] and applied without data-aiding after the definition of a unified signal model in [21]. In addition, a very preliminary study of the JML in LTE for a very specific scenario is presented in [22]. Therefore, the joint estimation algorithms found in the literature have mainly focused on communication applications, where a very accurate time-delay estimation is not critical in general. In our ranging application, the representation of the channel has to be improved, especially for those scenarios where multipath highly deteriorates the time-delay estimation. Thus, the channel estimation models have to be adapted to these harsh environments.

The periodic-tap estimation model is suitable for mass-market receivers, such as mobile phones, because it has a low complexity. However, this model may lead to significant ranging errors with close-in multipath. Typically, multipath appears close to the line-on-sight ray in urban and indoor environments, producing a critical degradation in ranging applications. This multipath, which is ignored in communications, significantly affects the performance of the periodic-tap estimation model for low-sampling rates, because short-delay multipath may not be properly modelled between samples. Therefore, we propose a hybrid estimation model by using equi-spaced taps together with an arbitrary tap between the first two. This solution improves the characterization of the channel while only adding the complexity of one more estimation parameter. Thus, the introduction of this arbitrary tap with a variable position helps to increase the ranging accuracy in close-in multipath environments. This new hybrid JML approach, as well as the periodic JML

approach, is studied in this paper and used to assess the achievable positioning performance of LTE, considering a low-complexity time-delay estimation that exploits the structure of the LTE OFDM signals. This estimation is analyzed for usual working conditions, represented by typical LTE signal bandwidths with the ETU standard channel model.

The remainder of this paper is organized as follows. Section 2 defines the signal model and describes the main LTE pilot signals. Section 3 defines the propagation channel model. Section 4 reviews the different channel estimation models and derives the joint ML estimator, including the novel channel parameterization. In Section 5, the performance of the joint ML estimators is assessed with numerical results in multipath and noise channels for different signal bandwidths. Finally, conclusions are drawn in Section 6.

## 2 Signal model

The downlink transmission of the LTE mobile communications standard is based on the OFDM modulation, whose complex-valued baseband representation is given by:

$$x_c(t) = \sqrt{\frac{2C}{N}} \sum_{n=0}^{N-1} b(n) \cdot \exp\left(j\frac{2\pi nt}{T}\right), \quad (1)$$

where  $C$  is the power of the band-pass signal,  $N$  is the total number of subcarriers,  $b(n)$  is the complex-valued symbol transmitted at the  $n$ th subcarrier, and  $T$  is the OFDM symbol period. The symbol  $b(n)$  is defined by  $b(n) = d(n) \cdot p(n)$ , being  $d(n)$  the data or pilot symbol assigned with a relative power weight  $p(n)^2$ , which is constrained by  $\sum_{n=0}^{N-1} p(n)^2 = N$ . In particular, the downlink physical layer of the LTE specification [1] defines a symbol period  $T$  of 66.67  $\mu$ s, which corresponds to a subcarrier spacing  $F_{sc} = 1/T$  of 15 kHz. The transmission grid is defined in time and frequency by resource blocks (RB), which are the minimum resource allocation unit formed by seven OFDM symbols and 12 subcarriers in the normal cyclic prefix configuration. The system bandwidth is scalable from 1.4 to 20 MHz, but the guard bands are left at the edges of the spectrum; thus, only a minimum transmission bandwidth of 6 RB (i.e. 1.08 MHz) and a maximum of 100 RB (i.e. 18 MHz) can be configured [6].

Assuming the successful removal of the cyclic prefix and perfect carrier frequency synchronization, the baseband received signal is

$$y_c(t) = x_c(t) * h_c(t) + n_c(t), \quad (2)$$

where  $*$  is the convolution operation,  $h_c(t)$  is an unknown channel impulse response (CIR), and  $n_c(t)$  is the white Gaussian noise. If the LTE receiver applies a sampling

frequency  $F_s$ , defined by the sampling period  $T_s = 1/F_s = T/N$ , the discrete-time signal model is

$$x_d(m) \doteq x_c(mT_s) = \sqrt{\frac{2C}{N}} \sum_{n=0}^{N-1} b(n) \exp\left(j\frac{2\pi nm}{N}\right), \quad (3)$$

where the discrete-time channel is  $h_d(m) \doteq h_c(mT_s)$ , the white Gaussian noise samples  $n_d(m) \doteq n_c(mT_s)$  are statistically uncorrelated with  $n_d(m) \sim \mathcal{N}(0, \sigma_n^2)$ , and the discrete-time received signal is  $y_d(m) \doteq y_c(mT_s)$ . After applying an  $N$ -point discrete Fourier transform (DFT) to  $y_d(m)$ , we have

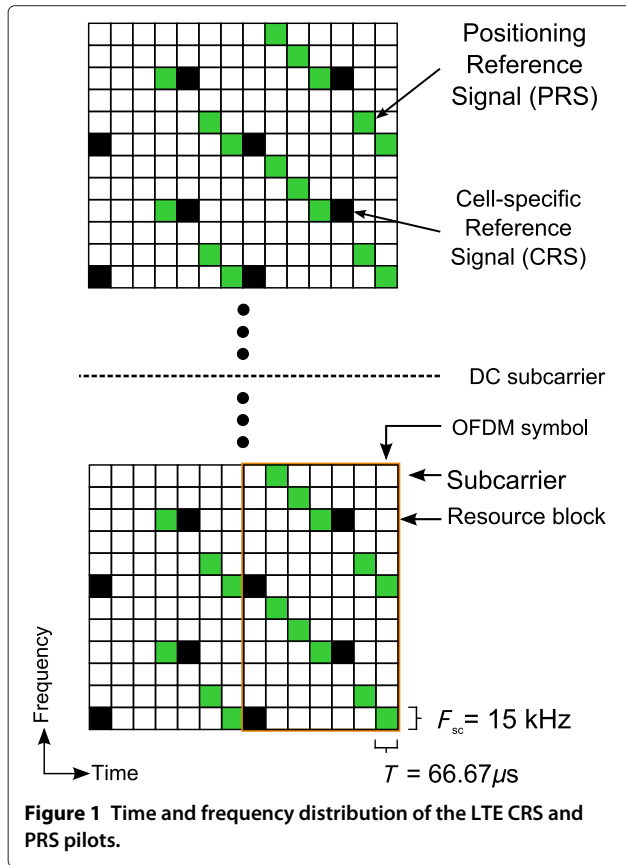
$$r(n) = \sqrt{2C} \cdot b(n) \cdot H(n) + w(n), \quad (4)$$

where  $n$  is the index of the subcarriers,  $H(n) = \mathcal{F}\{h_d(m)\}$  is the channel frequency response, being  $\mathcal{F}\{\cdot\}$  the discrete Fourier transform operator, and  $w(n)$  are the noise frequency samples, which are statistically uncorrelated with  $w(n) \sim \mathcal{N}(0, \sigma_w^2)$ .

The LTE pilot signals are constituted by the synchronization signals and the reference signals. The primary and secondary synchronization signals (i.e. PSS and SSS, respectively) are allocated in the centre of the spectrum with 62 contiguous pilot subcarriers, and avoiding the DC subcarrier. On the other hand, the reference signals, such as the cell-specific reference signal (CRS), are scattered in time and frequency spanning the maximum bandwidth of the configuration under use. Among the different pilot signals, the PRS is of special interest because its coordinated transmission avoids the inter-cell interference from neighbour cells, which is produced due to the single-frequency transmission. The pilot distribution of the CRS and PRS is shown in Figure 1. It should be noticed that the total number of subcarriers  $N$  defined in the signal model is equivalent to the bandwidth occupied by the active subcarriers, i.e. effective bandwidth. Using only the reference signals, the equivalent bandwidth is defined by  $N = 12 \cdot N_{RB} - 4$ , where  $N_{RB}$  is the number of resource blocks. As an example, let us consider that 6 RB and uniform power distribution among pilots subcarriers are used. Then, the normalized power spectral density of one PRS symbol without data transmission is shown in Figure 2. The total number of subcarriers  $N$  is equal to 68 subcarriers, which is equivalent to the effective bandwidth.

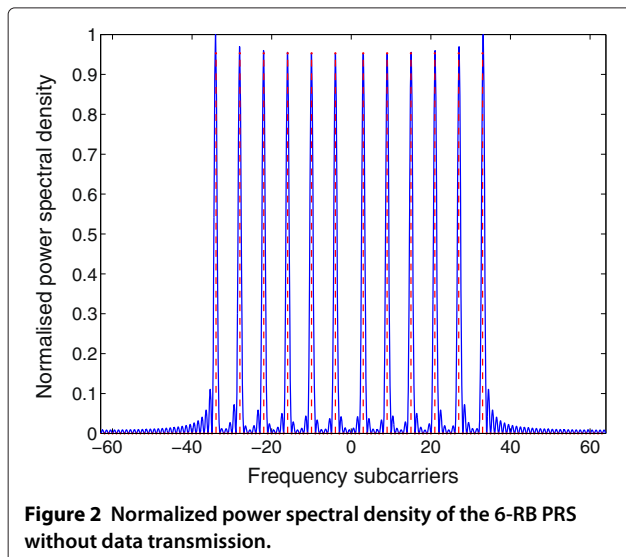
## 3 Propagation channel model

Propagation channel models are aimed to realistically represent the physical channel. In this sense, the multipath CIR is typically modelled by defining a tap for each physical ray. Every tap is determined by a complex amplitude and a time delay. In mobile communications, the standard multipath models for single-antenna transmission are the so-called tapped-delay line models [23]. Indeed, the LTE technology adopts specific TDL models inherited from



second- and third-generation mobile communications, i.e. GSM and UMTS, which are extended to cover the wide bandwidths of LTE signals. Following the TDL model, the propagation channel model shown in (2) is defined as

$$h_c(t) = \sum_{k=0}^{L_c-1} h_k \cdot \delta(t - t_k - t_e), \quad (5)$$



where  $L_c$  is the number of taps of the channel,  $h_k$  is the complex gain for the  $k$ th path,  $\delta(t)$  is the Dirac delta,  $t_k$  is the tap delay relative to the first tap (i.e.  $t_0 = 0$ ), and  $t_e$  is the time delay introduced by the channel (i.e. the time delay of the first arriving ray). The power-delay profile of the LTE TDL models is defined in Annex B of [6] and [7], by specifying the fixed delay  $t_k$  and relative average power  $\overline{RP}_k$  for every tap. The channel coefficients  $h_k$  of these extended models are time-varying with a Rayleigh distribution, and following a classical Jakes Doppler spectrum  $S(f)$ ,

$$S(f) \propto \sqrt{\frac{1}{1 - (f/f_D)^2}}, \quad \text{for } f \in [-f_D, f_D], \quad (6)$$

being  $f_D$  the maximum Doppler shift. Among these models, our interest is focused on the ETU channel model, whose parameters are shown in Table 1. As it can be noticed, the ETU model is characterized by a large delay spread of 5  $\mu s$  and strong multipath rays. Thus, the maximum average energy of the CIR may be located far from the time delay of the first arriving path. This deviation causes a notable degradation on the performance of the conventional TDE. The reason is that the matched filter estimates the time delay based on the maximum peak of the correlation, which coincides with the maximum energy of the CIR. Since the strongest correlation peak may not correspond to the first arriving path, a bias is produced on the time-delay estimation. Therefore, the ETU model defines a harsh environment, where the performance of the conventional estimator is relatively poor.

## 4 Time-delay estimation

### 4.1 Channel estimation models

It is important to note that channel estimation models should be distinguished from propagation channel models. The first ones consider the response of the channel in order to later counteract its effect. The second ones model the physical channel to understand the behaviour of the channel itself. Thus, the propagation channel models are

**Table 1** ETU channel model parameters

Tap $k$	$t_k$ (ns)	$\overline{RP}_k$ (dB)
1	0	-1.0
2	50	-1.0
3	120	-1.0
4	200	0.0
5	230	0.0
6	500	0.0
7	1,600	-3.0
8	2,300	-5.0
9	5,000	-7.0

used to simulate the actual channel, while the channel estimation models are used to represent the effect of the channel on the time-delay estimation. Next, we describe those channel estimation models that are typically used, as well as a new model presented in this work.

#### 4.1.1 Single-tap model

The most simple and used channel estimation model is the single-tap model. It assumes that the signal is just attenuated and delayed by the channel. Thus, this estimation model is only defined by a single-channel coefficient  $h_0$ , which can be complex-valued, associated to the propagation time delay  $t_e$ . Using a bandlimited representation for the channel, the discrete CIR of this model is

$$h_{ST}(m) = h_0 \cdot \text{sinc}(m - \tau), \quad (7)$$

where  $\text{sinc}(x) = \frac{\sin(\pi x)}{\pi x}$  is the sinc function, and  $\tau \doteq t_e/T_s$  is the discrete-time symbol-timing error, which is the time delay to estimate. This estimation model is typically applied in AWGN channels. Using this model, the derivation of the ML estimator results in the correlation-based estimator. As it was discussed at the end of

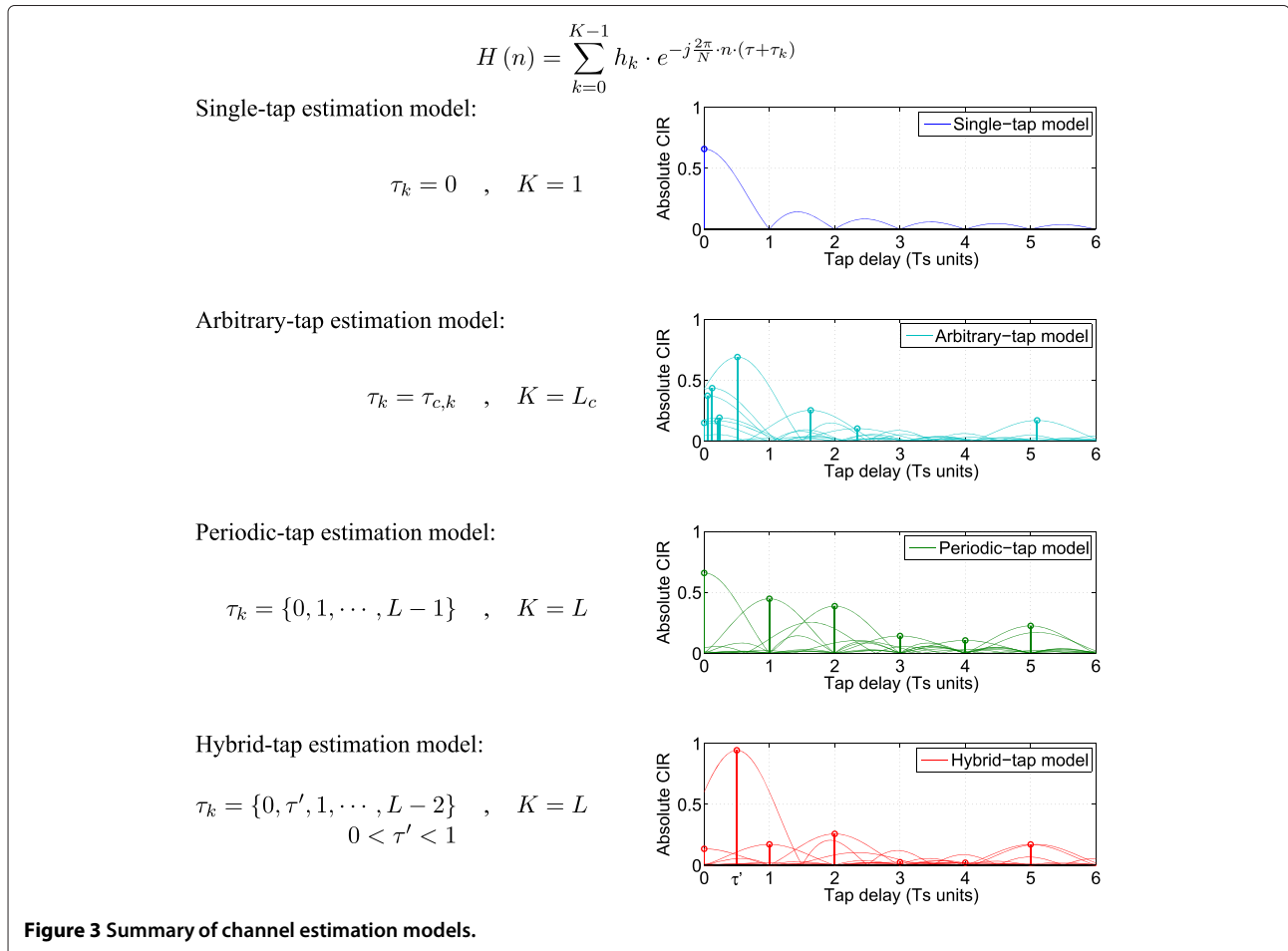
Section 3, this conventional TDE has a considerable bias in multipath channels. The main characteristics of this channel model are shown in Figure 3.

#### 4.1.2 Arbitrary-tap model

The most accurate model is constituted by the amplitude, phase and delay of every physical multipath ray. However, this model is also the most complex because these parameters have to be estimated for every tap. Since the taps' delays are in positions to be determined, this model is hereafter called the arbitrary-tap model. Its discrete CIR is written as

$$h_{AT}(m) = \sum_{k=0}^{L-1} h_k \cdot \text{sinc}(m - \tau_k - \tau), \quad (8)$$

where  $L$  is the number of taps,  $h_k$  is the channel coefficient for the  $k$ th tap,  $\tau_k$  is the relative delay to the first tap (i.e.  $\tau_0 = 0$ ), and  $\tau$  is the time delay. As it shown in Figure 3, the arbitrary-tap model is represented, in that case, by matching the  $L_c$  propagation taps at delay positions  $\tau_{c,k}$ . Although the channel response can be accurately reconstructed using this model, the implementation



complexity is a major concern. For instance, the number of unknowns substantially increases (without *a priori* statistics) in dense multipath due to the high number of rays to estimate. Thus, the iterative methods implemented for the TDE, such as super-resolution techniques [10], have a high computational burden.

#### 4.1.3 Periodic-tap model

The complexity of the channel estimation model is reduced by placing the estimation taps in equi-spaced or periodic delay positions. The aim is to avoid the tap delay estimation for every physical ray and focus on the propagation time-delay estimation. Thus, the actual physical tap positions are not estimated, and the resulting model is a sampled version of the channel impulse response. The discrete CIR of the periodic-tap model is

$$h_{PT}(m) = \sum_{k=0}^{L-1} h_k \cdot \text{sinc}(m - k - \tau), \quad (9)$$

where  $L$  is the number of taps,  $h_k$  is the channel coefficient for the  $k$ th tap, and  $\tau$  is the time delay. Ideally, the sampled model would require an infinite number of taps in order to perfectly represent the channel. The solution described in (9) is to truncate the number of taps to  $L$ , by assuming that the rest of taps have a negligible contribution. However, this assumption may produce an incorrect characterization of the channel response, leading to the so-called problem of model mismatch. The periodic-tap model is represented in the example of Figure 3 considering six taps. Since the tap positions are assumed to be equi-spaced, the close-in multipath, i.e. multipath close to the LoS signal, is not properly modelled when it appears between the first two samples at delay 0 and  $T_s$ . Thus, the multipath energy missed between samples may severely degrade the performance of the time-delay estimation. In the opposite case, if the sampling period  $T_s$  is small enough, the number of taps  $L$  has to expand a similar interval to the multipath dispersion. The design of  $L$  is beyond the scope of the paper, but it can be obtained by means of model order selection techniques, such as minimum description length (MDL) or Akaike [16], or by considering the delay spread of the channel, which can be estimated as in [24] and the references therein.

#### 4.1.4 Hybrid-tap model

A novel hybrid solution is proposed in this paper by using the equi-spaced taps together with an additional tap in a position to be determined between the first two. Thus, the equi-spaced taps allow the estimator to capture most of the multipath energy present in the propagation model, while the additional tap models close-in multipath with only the added complexity of having one more variable. The CIR of the hybrid-tap model is defined as

$$h_{HT}(m) = \sum_{k=0}^{L-2} h_k \cdot \text{sinc}(m - k - \tau) + h_{L-1} \cdot \text{sinc}(m - \tau' - \tau), \quad 0 < \tau' < 1, \quad (10)$$

where  $L$  is the number of taps,  $h_k$  is the channel coefficient for the  $k$ th periodic tap,  $h_{L-1}$  and  $\tau'$  denote the channel coefficient and delay of the arbitrary tap, respectively, and  $\tau$  is the time delay. As an example, the hybrid-tap model is represented in Figure 3, where the arbitrary-tap delay values of  $\tau'$  are fixed within 0 and 1 with respect to  $\tau$ .

#### 4.2 One-dimensional joint ML estimator

In order to derive a low-complexity time-delay estimator, the periodic-tap model is first selected. Thus, the estimation parameters are the time delay  $\tau$  and the channel coefficients  $\mathbf{h} = [h_0, \dots, h_{L-1}]^T$ . The received signal of (4) can be rewritten in matrix notation as in [20-22],

$$\mathbf{r} = \mathbf{B}\Gamma_\tau \mathbf{F}_L \mathbf{h} + \mathbf{w}, \quad (11)$$

where

$$\mathbf{r} = [r(-N/2 + 1), \dots, r(N/2)]^T, \quad (12)$$

$$\Gamma_\tau = \text{diag}\left(e^{-j\frac{2\pi}{N}(-N/2+1)\tau}, \dots, e^{-j\frac{2\pi}{N}(N/2)\tau}\right), \quad (13)$$

$$\mathbf{B} = \sqrt{2C} \cdot \text{diag}(b(-N/2 + 1), \dots, b(N/2)), \quad (14)$$

$$\mathbf{h} = [h_0, \dots, h_{L-1}]^T, \quad (15)$$

$$\mathbf{w} = [w(-N/2 + 1), \dots, w(N/2)]^T, \quad (16)$$

and  $\mathbf{F}_L$  is composed of the first  $L$  columns of the zero-frequency-centred  $N \times N$  DFT matrix,

$$\mathbf{F}_L = \frac{1}{\sqrt{N}} \begin{bmatrix} 1 & \omega^{-\frac{N}{2}+1} & \dots & \omega^{(-\frac{N}{2}+1)(L-1)} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & 1 & \dots & 1 \\ 1 & \omega & \dots & \omega^{L-1} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & \omega^{\frac{N}{2}} & \dots & \omega^{\frac{N}{2}(L-1)} \end{bmatrix}, \quad (17)$$

where  $\omega = e^{-j\frac{2\pi}{N}}$ . Let us define a matrix  $\mathbf{A}$  of dimensions  $N \times L$  as a function of  $\tau$  as follows:

$$\mathbf{A}_\tau = \mathbf{B}\Gamma_\tau \mathbf{F}_L. \quad (18)$$

Hence, the received signal is expressed as

$$\mathbf{r} = \mathbf{A}_\tau \mathbf{h} + \mathbf{w}. \quad (19)$$

Given this formulation, the maximum likelihood criterion is applied, which results in

$$\begin{bmatrix} \hat{\tau} \\ \hat{\mathbf{h}} \end{bmatrix} = \arg \max_{\tau, \mathbf{h}} \Lambda(\mathbf{r}; \tau, \mathbf{h}), \quad (20)$$

where  $\Lambda(\mathbf{r}; \tau, \mathbf{h})$  is the likelihood function of the received samples parameterized by the unknowns  $\tau$  and  $\mathbf{h}$ , which is defined by a multivariate Gaussian distribution,

$$\Lambda(\mathbf{r}; \tau, \mathbf{h}) = C_0 \exp\left(-\frac{1}{\sigma_w^2} \|\mathbf{r} - \mathbf{A}_\tau \mathbf{h}\|^2\right), \quad (21)$$

being  $C_0$  an irrelevant constant. Substituting the log-likelihood function in (20) leads to the following minimization problem:

$$\begin{bmatrix} \hat{\tau} \\ \hat{\mathbf{h}} \end{bmatrix} = \arg \min_{\tau, \mathbf{h}} \{\|\mathbf{r} - \mathbf{A}_\tau \mathbf{h}\|^2\}, \quad (22)$$

which coincides with the nonlinear least squares (NLS) criterion, since  $\tau$  depends nonlinearly on the received signal model. The resulting two-dimensional optimization can be separated by minimizing first with respect to  $\mathbf{h}$  and then with respect to  $\tau$  as in [25], which can be written as

$$\hat{\tau} = \arg \min_{\tau} \left\{ \min_{\mathbf{h}} \|\mathbf{r} - \mathbf{A}_\tau \mathbf{h}\|^2 \right\}. \quad (23)$$

Then, the well-known least-squares solution can be applied to obtain the ML estimate of the unknown channel coefficients as

$$\hat{\mathbf{h}} = \mathbf{A}_\tau^\dagger \mathbf{r}, \quad (24)$$

where  $\mathbf{A}_\tau^\dagger$  denotes the Moore-Penrose pseudo-inverse of  $\mathbf{A}_\tau$ , which is defined as

$$\mathbf{A}_\tau^\dagger \doteq (\mathbf{A}_\tau^H \mathbf{A}_\tau)^{-1} \mathbf{A}_\tau^H, \quad (25)$$

being the superindex  $H$  the Hermitian conjugate. Introducing the least-squares solution into (23), the ML estimation of the time delay results in

$$\hat{\tau} = \arg \min_{\tau} \left\{ \|\mathbf{r} - \mathbf{A}_\tau \mathbf{A}_\tau^\dagger \mathbf{r}\|^2 \right\} = \arg \min_{\tau} \left\{ \|\mathbf{P}_{\mathbf{A}_\tau}^\perp \mathbf{r}\|^2 \right\}, \quad (26)$$

where  $\mathbf{P}_{\mathbf{A}_\tau}^\perp = \mathbf{I} - \mathbf{A}_\tau (\mathbf{A}_\tau^H \mathbf{A}_\tau)^{-1} \mathbf{A}_\tau^H$  is the orthogonal projection matrix onto the subspace orthogonal to that spanned by the columns of  $\mathbf{A}_\tau$ . Thus, the decoupling of  $\hat{\tau}$  and  $\hat{\mathbf{h}}$  leads to the proposed ML time-delay estimator of (26). It is hereafter called *one-dimensional joint ML (1D-JML)* time-delay and channel estimator. The 1D-JML estimation is computed numerically by minimizing the cost function of  $\|\mathbf{P}_{\mathbf{A}_\tau}^\perp \mathbf{r}\|^2$  as a function of  $\tau$ . This optimization is not complex because it is a one-dimensional function that is simply evaluated within the range  $[-1/2, 1/2]$  and then minimized. This range is defined to find the residual time delay after a coarse estimation. The minimum could be obtained by solving the function with a sufficiently fine grid of points. However, the `fminbnd` function of MATLAB is used for an efficient computation, which finds the minimum in the search interval. Instead of doing

an exhaustive evaluation, this function searches the minimum by means of the golden section technique followed by a parabolic interpolation.

Let us study the particular case of  $L$  equal to 1. In this case, the channel is formed only by one ray, thus  $\mathbf{A}_\tau$  is a  $N \times 1$  matrix defined as  $\mathbf{A}_\tau = \mathbf{B} \Gamma_\tau \mathbf{F}_1$ . Developing further the expression of (26), the one-dimensional optimization problem results into the following maximization of the cost function:

$$\hat{\tau} = \arg \max_{\tau} \{|\mathbf{A}_\tau^H \mathbf{r}|^2\} = \arg \max_{\tau} \{|R(\tau)|^2\}, \quad (27)$$

where  $R(\tau)$  is the cross-correlation of the received signal  $\mathbf{r}$  with the pilot symbols  $\mathbf{b}$  defined in the scalar notation as

$$R(\tau) = \sum_{n=0}^{N-1} r(n) \cdot b^*(n) \cdot \exp\left(j \frac{2\pi n\tau}{N}\right). \quad (28)$$

Thus, the particular case of the 1D-JML estimation for  $L = 1$  reduces to the estimation based on the correlation or matched filter output. This confirms the optimality of the matched filter for time-delay estimation in the absence of multipath.

### 4.3 Two-dimensional joint ML estimator

The derivation of the JML estimator, using the periodic-tap channel estimation model described in (9), results in a low-complexity implementation by decoupling the problem of joint time-delay and channel estimation. Now, the hybrid-tap estimation model of (10) is applied to enhance the characterization of the physical channel response. Using this novel channel parameterization, the model mismatch is reduced at the expense of adding one more estimation parameter, the arbitrary-tap delay  $\tau'$ . Considering the derivation of the 1D-JML obtained in (26), the problem at hand is solved following the same procedure. This leads to the *two-dimensional joint ML (2D-JML)* estimator, which can be expressed as

$$\begin{bmatrix} \hat{\tau} \\ \hat{\tau}' \end{bmatrix} = \arg \min_{\tau, \tau'} \left\{ \|\mathbf{P}_{\mathbf{A}_{\tau, \tau'}}^\perp \mathbf{r}\|^2 \right\}, \quad (29)$$

s.t.  $0 < \tau' < 1$ ,

where  $\mathbf{P}_{\mathbf{A}_{\tau, \tau'}}^\perp = \mathbf{I} - \mathbf{A}_{\tau, \tau'} (\mathbf{A}_{\tau, \tau'}^H \mathbf{A}_{\tau, \tau'})^{-1} \mathbf{A}_{\tau, \tau'}^H$ , and  $\mathbf{A}_{\tau, \tau'} = \mathbf{B} \Gamma_\tau \mathbf{F}_{L, \tau'}$ , being the Fourier matrix  $\mathbf{F}_{L, \tau'}$  dependant also of  $\tau'$  as

$$\mathbf{F}_{L, \tau'} = \frac{1}{\sqrt{N}} \begin{bmatrix} 1 & \omega^{-\frac{N}{2}+1} & \dots & \omega^{(-\frac{N}{2}+1)(L-2)} & \omega^{(-\frac{N}{2}+1)\tau'} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 1 & 1 & \dots & 1 & 1 \\ 1 & \omega & \dots & \omega^{L-2} & \omega^{\tau'} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 1 & \omega^{\frac{N}{2}} & \dots & \omega^{\frac{N}{2}(L-2)} & \omega^{\frac{N}{2}\tau'} \end{bmatrix}. \quad (30)$$



The two-dimensional optimization of (29) is computed by an exhaustive search in the  $\tau \times \tau'$  region of  $[-1/2, 1/2] \times [0, 1]$ . Since the cost function of  $\|\mathbf{P}_{A,\tau,\tau'}^\perp \mathbf{r}\|^2$  only depends on two parameters, its minimum can be found with the required accuracy by evaluating the function in a sufficiently fine grid of points.

## 5 Numerical results

The proposed JML time-delay estimator is, in principle, applicable to any multicarrier signal. Multicarrier signals show a flexible allocation of data and pilot resources that facilitates the adoption of the JML estimator. Thus, the JML estimator is used to show the achievable performance with the LTE positioning reference signals for different signal bandwidths. The TDE performance of the 1D- and 2D-JML estimators for  $L > 1$  is compared with that of the 1D-JML estimator for  $L = 1$ , i.e. the conventional correlation-based technique. First, the multipath error envelope (MPEE) is used to characterize the multipath impact on the TDE. Second, the bias and the root-mean-square error (RMSE) of the JML estimators is statistically assessed over realistic multipath and noise conditions. In order to conduct these analyses, the OFDM signal is assumed to be successfully acquired, being the receiver in signal tracking mode, thus the time-delay estimation range is defined within  $[-T_s/2, T_s/2]$ , or  $[-1/2, 1/2]$  since  $\tau$  is in  $T_s$  units.

### 5.1 Multipath error envelope

The main properties of the proposed estimator can be studied through the MPEE. This metric evaluates the impact of a two-ray multipath model on the time-delay estimation. In the absence of noise, the MPEE represents the time-delay error produced by a multipath reflection (with specific delay, power and phase) when it is added to the LoS component. Thus, the received signal in the MPEE analysis is defined as

$$y_d(m) = x_d(m - \tau) + a_1 \cdot e^{j\phi_1} \cdot x_d(m - \tau - \tau_1), \quad (31)$$

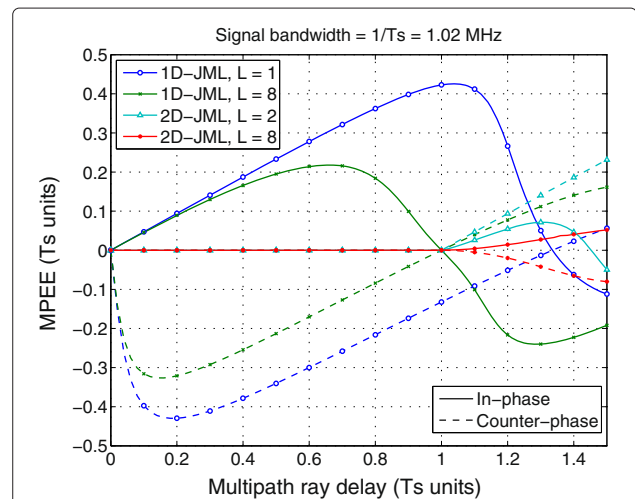
where  $a_1$ ,  $\phi_1$  and  $\tau_1$  are the amplitude, phase and delay of the multipath ray, respectively. The MPEE is computed considering  $-1$  dB of relative power to the LoS ray within a delay range between 0 and  $3 \cdot T_s/2$ . The multipath ray is added constructively and destructively to the LoS component, i.e. the multipath contribution is in-phase (i.e.  $\phi_1 = 0$ ) and counter-phase (i.e.  $\phi_1 = \pi$ ), respectively. In this scenario, the LTE PRS is configured for the lowest bandwidth of 6 RB, assuming no data allocation on the transmitted symbol. As it is discussed in Section 2, the 6-RB PRS bandwidth is defined by  $N = 12 \cdot N_{RB} - 4 = 68$  subcarriers, which results in  $T_s = T/N = 980.39$  ns and a signal bandwidth equal to  $1/T_s = 1.02$  MHz.

The resulting MPEE is shown in Figure 4, by comparing the 1D-JML estimator for  $L = \{1, 8\}$  with the 2D-JML estimator for  $L = \{2, 8\}$ , using expressions (27), (26) and (29), respectively. As it can be noticed, the multipath errors are normalized with respect to the sampling period  $T_s$ . It has been confirmed through simulations that the same relative results are obtained for higher signal bandwidths. Thus, the maximum errors  $\epsilon_{\max}$  of the 1D-JML estimator are calculated in metres for constructive and destructive cases using different sampling periods, as it is shown in Table 2. Three main results can be identified:

- The effect of increasing the number of taps from  $L = 1$  to  $L = 8$  in the 1D-JML estimator, that is, from using a single-tap model to a periodic-tap model, improves the TDE performance, but there is still a significant bias in both cases.
- While the 1D-JML estimator for  $L = \{1, 8\}$  is only unbiased at certain instants (e.g.  $\tau = \{1.34, 1\}$ , respectively), the 2D-JML estimator is completely unbiased for values of multipath delay  $\tau_1$  within 0 and 1 due to the matching between the channel estimation model and the propagation channel model.
- The effect of decreasing the number of taps from  $L = 8$  to  $L = 2$  in the 2D-JML estimator does not have the same behaviour as in the 1D-JML estimator because the hybrid approach is still unbiased for values of multipath delay  $\tau_1$  within 0 and 1.

### 5.2 Bias and RMSE of the JML estimators over realistic conditions

The multipath error envelope has shown the bias introduced by a particular multipath ray on the time-delay estimation. The results indicate the potential of the new JML



**Figure 4** MPEE of the 1D- and 2D-JML estimators using the 6-RB PRS without data transmission.



**Table 2 Maximum TDE errors of the 1D-JML in the MPEE**

Bandwidth (RB)	$T_s/2$ (m)	$\epsilon_{\max, L=1}$ (m)		$\epsilon_{\max, L=8}$ (m)	
		$\phi_1 = 0$	$\phi_1 = \pi$	$\phi_1 = 0$	$\phi_1 = \pi$
6	147.06	127.02	-127.07	64.71	-96.11
25	33.78	29.18	-29.19	14.87	-22.08
50	16.78	14.49	-14.50	7.38	-10.97

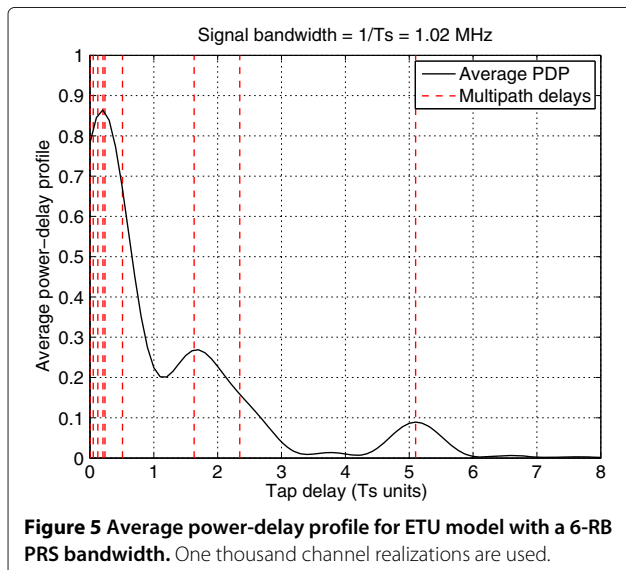
approach to improve the TDE performance with respect to the conventional correlator-based estimator. However, the two-ray multipath model does not represent general urban channels. Thus, the ETU channel model is used to assess the performance of the estimators in more realistic conditions.

### 5.2.1 Low signal bandwidth (i.e. 1.4 MHz)

The effect of multipath on the time-delay estimation is first assessed statistically considering the ETU model and the lowest LTE bandwidth of 1.4 MHz. Within this bandwidth, the PRS is allocated along 6 RB without data transmission, which results in a signal bandwidth equal to  $1/T_s = 1.02$  MHz. For this case, 1,000 ETU realizations are computed with a Doppler shift of 500 Hz. The resulting channel is represented with the average power-delay profile  $\overline{\text{PDP}}$  in Figure 5. The average PDP is calculated with the mean absolute value of the discrete CIR for every  $\ell$ th realization  $h_\ell(m)$  in the interval  $[\tau, \tau + 8]$ , that is,

$$\overline{\text{PDP}}(m) = \frac{1}{N_\ell} \cdot \sum_{\ell=0}^{N_\ell-1} |h_\ell(m)|^2, \quad \tau < m < \tau + 8, \quad (32)$$

where  $N_\ell$  is the number of realizations. In Figure 5, the multipath delays of the channel are highlighted with

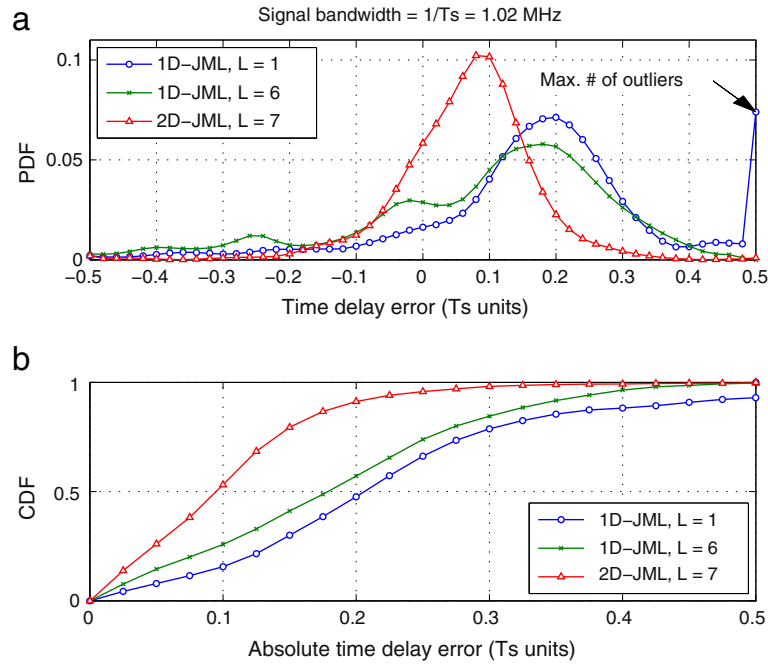


vertical red lines. As it can be seen, this channel model is mainly characterized by the presence of LoS signal and strong multipath in short delays. Thus, most of the multipath energy is concentrated for delays between 0 and  $T_s/2$ , approximately. In addition, it can be seen (as specified in Table 1) that the delay spread of the ETU model is equal to  $5.1 \cdot T_s$ . Then, if the periodic-tap estimation model is used, one can notice as the estimation taps at positions larger than the delay spread have a negligible multipath contribution. Thus, we use this prior information in order to correctly assume the truncation of the number of taps to the delay spread of the ETU model, which in the 1D-JML estimator corresponds to  $L = 6$  and in the 2D-JML estimator corresponds to  $L = 7$ . Using a higher number of taps, the estimators do not capture more channel energy, thus they may obtain a similar TDE performance (in absence of noise).

Given the generated ETU channel, time-delay errors are computed in the absence of AWG noise using the 1D- and 2D-JML estimators. The probability density function (PDF) of the resulting time-delay errors is shown in Figure 6a. The performance of the 1D-JML estimator for  $L = 1$  is poor, producing the highest number of outliers. The outlier estimations are defined as those time-delay estimations with an absolute error higher or equal to  $T_s/2$ , which are then truncated to  $T_s/2$ . In this sense, the application of the periodic-tap estimation model (with six taps) reduces the number of outliers. Nevertheless, the low sampling rate avoids this channel estimation model to properly characterize close-in multipath. Thus, using the new hybrid-tap estimation model, an additional arbitrary tap is introduced between 0 and  $T_s$  to reduce the model mismatch. The resulting 2D-JML estimator shows a notable improvement with respect to the 1D-JML estimators. This enhancement is highlighted by the cumulative density function (CDF) of the absolute time-delay error, shown in Figure 6b. For instance, the 2D-JML estimator for  $L = 7$  produces an absolute TDE error of  $0.12 \cdot T_s$  (i.e. 35.3 m) for 67% of the cases, while the 1D-JML estimators obtain (for the same percentage of the cases) an error of  $0.25 \cdot T_s$  (i.e. 73.5 m) with  $L = 1$  and  $0.23 \cdot T_s$  (i.e. 67.7 m) with  $L = 6$ . Thus, the 2D-JML estimator provides an important reduction of the multipath error.

Once the impact of multipath has been assessed, AWG noise is added to the ETU channel model. The signal-to-noise ratio (SNR) takes values between  $-20$  and  $30$  dB. For each SNR value, 1,000 ETU model realizations are processed. The time-delay errors (including the truncated outliers) obtained by the JML estimators for every SNR are used to compute the root-mean-square error, defined as

$$\text{RMSE}(\hat{\tau}) = \sqrt{\text{E}[(\hat{\tau} - \tau)^2]}, \quad (33)$$



**Figure 6** Performance of 1D- and 2D-JML estimators using ETU model without noise and 6-RB PRS bandwidth. **(a)** Probability density function of the time-delay estimations. **(b)** Cumulative density function of the time-delay estimations. One thousand channel realizations are used.

and the bias, expressed as

$$b(\hat{\tau}) = E[\hat{\tau}] - \tau, \quad (34)$$

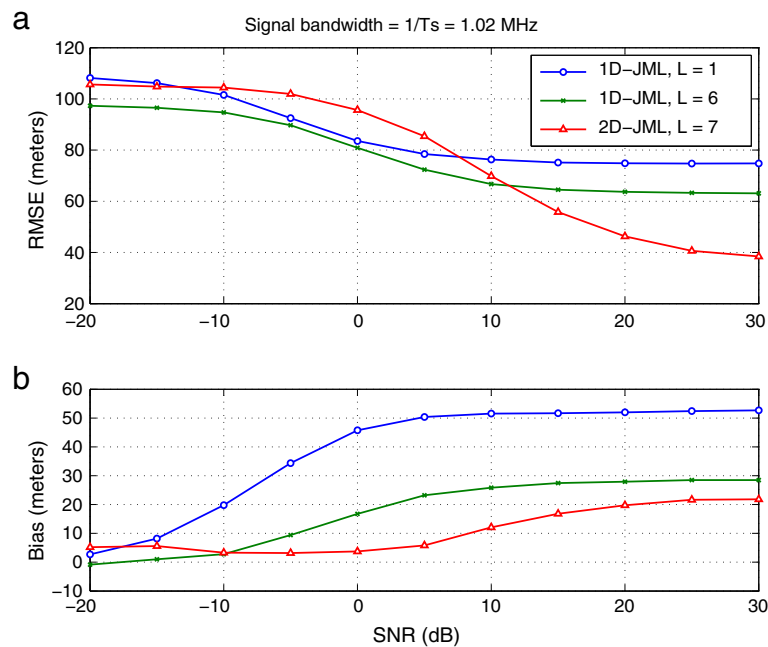
being  $E[\cdot]$  the expectation operator. Considering both multipath and noise, the RMSE of the estimators is depicted in Figure 7a, whereas the bias of the estimators is shown in Figure 7b, being both metrics expressed in metres. Since the multipath channel changes every ETU realization, the RMSE and bias are not equal for high SNR. The lowest bias, i.e. 21.7 m, is achieved by the 2D-JML estimator for  $L = 7$  at high-SNR values, such as 30 dB. It obtains a major improvement with respect to the 1D-JML estimator for  $L = 1$  (i.e. conventional TDE), whose minimum bias is equal to 52.7 m. In addition, the new hybrid estimation reduces the model mismatch error, since the 1D-JML estimator for  $L = 6$  has a bias of 28.6 m at 30 dB of SNR. Nevertheless, the 2D-JML estimator is more affected by noise than the 1D-JML estimators, which results in a higher RMSE at low SNR values. This is due to the fact that the variance of the joint ML estimation increases with the number of unknown parameters to estimate. Thus, there is a trade-off between the efforts to counteract multipath and the robustness against noise.

### 5.2.2 Typical signal bandwidths (i.e. 5 and 10 MHz)

The most usual working modes of LTE are based on the 5 and 10 MHz operating bandwidths. These configurations can be identified as typical modes because they are specified for most of the LTE bands, as it is shown in

Table 5.6.1-1 of [6]. The signal bandwidths associated to these modes are 25 RB (i.e. 4.5 MHz) and 50 RB (i.e. 9 MHz), respectively. Thus, the ETU model is applied with these typical bandwidths in order to represent usual LTE positioning conditions.

Using the ETU model realizations of the previous section, the average PDP is shown for both bandwidths in Figure 8. The range of the tap delay is defined between 0 and 1.96  $\mu$ s, which coincides with  $2 \cdot T_s$  for a 6-RB bandwidth. For the current bandwidths, the sampling period  $T_s$  is 225 ns for 25 RB and 112 ns for 50 RB, given a total number of  $N$  subcarriers equal to 296 and 596, respectively. Thus, the time-delay estimation can be focused on the short-delay multipath. Given a higher channel bandwidth, the contribution of every multipath ray is more independent. In the same way, the sampling rate of the estimation model is higher, and more multipath energy can be captured by every estimation tap. Therefore, the 1D- and 2D-JML estimators can use a number of taps  $L$  lower than the delay spread of the channel. For a 25-RB bandwidth, we should consider  $L = 8$  for the 1D-JML estimator and  $L = 9$  for the 2D-JML estimator, while for a 50-RB bandwidth, we should consider  $L = 4$  for the 1D-JML estimator and  $L = 5$  for the 2D-JML estimator. *A priori* information of the average PDP should be used to minimize the number of taps  $L$  according to the most significant amount of energy of the channel in order to alleviate the computational burden of the estimation.

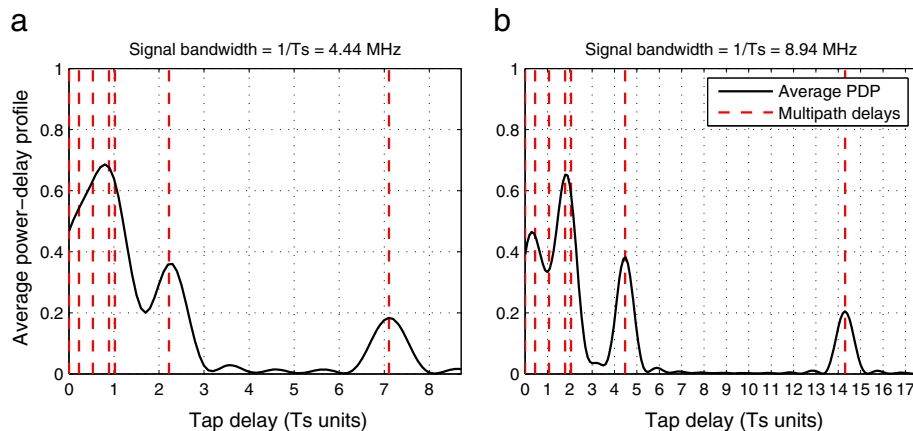


**Figure 7** Performance of 1D- and 2D-JML estimators using ETU model with AWGN and 6-RB PRS bandwidth. **(a)** Root-mean-square error of the time-delay estimations. **(b)** Bias of the time-delay estimations. One thousand ETU model realizations per SNR are used.

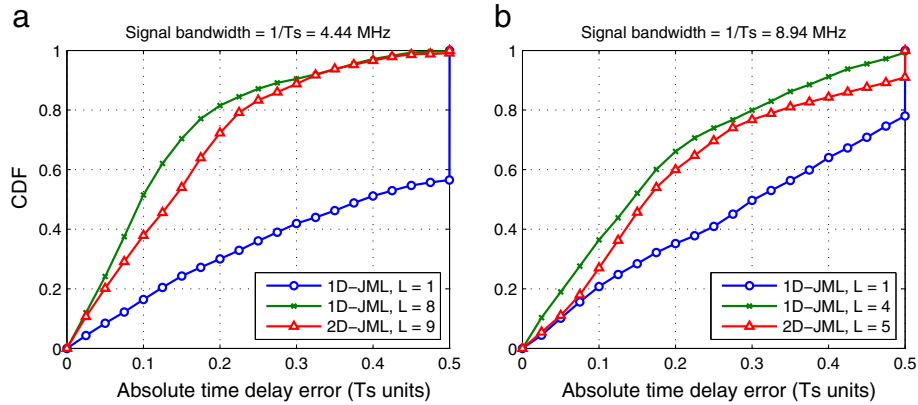
The cumulative density function of the TDE errors obtained with the 1D- and 2D-JML estimators is compared using both bandwidths in Figure 9. As it can be seen, the 1D- and 2D-JML estimators for  $L > 1$  improve the TDE performance with respect to the 1D-JML estimator for  $L = 1$  in both cases. In particular, there is a higher gain for 25-RB bandwidth than for 50-RB bandwidth. This is due to the fact that the estimation tap delays are changed with the sampling period. The best TDE performance is achieved when the estimation taps capture most of the multipath energy. In the cases under study, the periodic-tap 1D-JML estimator for  $L > 1$  performs slightly better

than the hybrid-tap 2D-JML estimator for  $L > 1$ . However, both estimators still achieve a very accurate ranging performance.

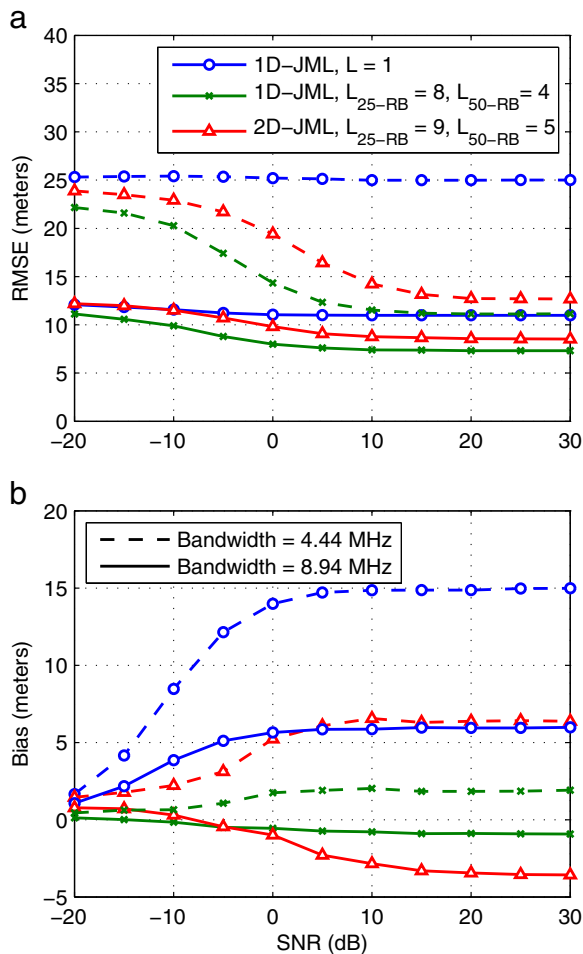
Considering the process followed in the previous section, the impact of multipath and noise is assessed for the typical signal bandwidths. The RMSE and the bias of the 1D- and 2D-JML estimators for  $L > 1$  outperform the 1D-JML estimator for  $L = 1$ , as shown in Figure 10. Indeed, it is essential to use  $L > 1$  with 25-RB bandwidth in order to obtain a satisfactory performance. As it can be seen in the figure, the 1D-JML estimator for  $L > 1$  achieves a slightly lower RMSE than the 2D-JML



**Figure 8** Average power-delay profile for ETU model. **(a)** 25-RB PRS bandwidth. **(b)** 50-RB PRS bandwidth. One thousand channel realizations are used.



**Figure 9** CDF of the 1D- and 2D-JML time-delay estimations using ETU model without noise. (a) 25-RB PRS bandwidth. (b) 50-RB PRS bandwidth. One thousand channel realizations are used.



**Figure 10** Performance of 1D- and 2D-JML estimators using ETU model with AWGN and {25,50}-RB PRS bandwidth. (a) Root-mean-square error of the time-delay estimations. (b) Bias of the time-delay estimations. One thousand ETU model realizations per SNR are used.

estimator for  $L > 1$  in both bandwidth cases. However, this difference between the 1D- and 2D-JML estimators for  $L > 1$  on the RMSE is as low as within 2 m for both bandwidths. Considering the 50-RB PRS bandwidth (i.e. 8.94 MHz), the bias of both 1D-JML estimator for  $L = 4$  and 2D-JML estimator for  $L = 5$  is below 5 m. Thus, the JML estimation using the periodic-tap model and the novel hybrid-tap model exploits the LTE performance with a notable improvement with respect to the JML estimation using the single-tap model (i.e. matched filter or correlator), achieving a promising accuracy in usual working conditions.

## 6 Conclusions

A new technique for joint time-delay and channel estimation is presented in this paper to improve the ranging performance in channels with close-in multipath. The proposed algorithm is a joint maximum likelihood (JML) time-delay and channel estimator based on a new hybrid channel estimation model, defined by equi-spaced or periodic taps and an arbitrary tap between the first two. This novel channel parameterization helps to counteract short-delay multipath by solving a two-dimensional optimization problem with relative low complexity. The technique has been studied for the specific case of positioning in LTE, using the positioning reference signal (PRS). The results have been obtained in usual LTE working conditions, represented by the standardized ETU channel model and typical LTE signal bandwidths of 1.4, 5 and 10 MHz. The hybrid approach significantly improves the ranging performance for the lowest signal bandwidth (i.e. 1.4 MHz), where close-in multipath is critical, with respect to the periodic approach (i.e. only equi-spaced taps) and the conventional correlation-based estimator. For high signal bandwidths, such as 10 MHz, both hybrid and periodic JML estimators still provide

smaller time-delay estimation errors than the matched filter, achieving a bias below 5 m.

#### Competing interests

The authors declare that they have no competing interests.

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#### Disclosure

The content of the present article reflects solely the authors view and by no means represents the official ESA view.

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